

Part II

a) $V_k = 150 \text{ kV}$

$S_b = 100 \text{ MVA}$

$P_G = 0,9 \text{ pu}$

$P_S = -0,9 \text{ pu}$

$P_1 = 0$

$$X_{L3} = X_{L1} = \omega l d = 100 \cdot \pi \cdot 1,2 \times 10^{-3} \cdot 100 = 37,699 \Omega = 0,1675 \text{ pu}$$

$$X_{L2} = 2 \omega l d = 2 X_{L1} = 75,398 \Omega = 0,335102 \text{ pu}$$

$$[-B] = \begin{bmatrix} \frac{1}{X_{L1}} + \frac{1}{X_{L2}} & -\frac{1}{X_{L1}} & -\frac{1}{X_{L2}} \\ -\frac{1}{X_{L1}} & \frac{1}{X_{L1}} + \frac{1}{X_{L3}} & -\frac{1}{X_{L3}} \\ -\frac{1}{X_{L2}} & -\frac{1}{X_{L3}} & \frac{1}{X_{L2}} + \frac{1}{X_{L3}} \end{bmatrix}$$

$$\begin{bmatrix} \theta_2 \\ \theta_3 \end{bmatrix} = [-B]^{-1} \cdot \begin{bmatrix} P_2 \\ P_3 \end{bmatrix} = \begin{bmatrix} \frac{1}{X_{L1}} + \frac{1}{X_{L2}} & -\frac{1}{X_{L3}} \\ -\frac{1}{X_{L3}} & \frac{1}{X_{L2}} + \frac{1}{X_{L3}} \end{bmatrix}^{-1} \cdot \begin{bmatrix} 0,9 \\ -0,9 \end{bmatrix} = \begin{bmatrix} 0,037699 \\ -0,075398 \end{bmatrix}$$

$\theta_1 = 0$

$\theta_2 = 0,037699$

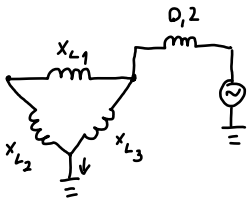
$\theta_3 = -0,075398$

$$P_{12} = \frac{\theta_1 - \theta_2}{X_{L1}} = -0,225 \text{ pu} = -22,5 \text{ MW}$$

$$P_{23} = \frac{\theta_2 - \theta_3}{X_{L3}} = 0,675 \text{ pu} = 67,5 \text{ MW}$$

$$P_{13} = \frac{\theta_1 - \theta_3}{X_{L2}} = -0,225 \text{ pu} = -22,5 \text{ MW}$$

b)



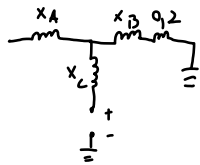
$$S_{cc} = V_0 \cdot I_{cc} = \frac{V_0^2}{x_{th}} = \frac{1}{x_{th}} = 3,07 \text{ pu} \rightarrow 307 \text{ MVA}$$

$V_0 = 1 \text{ pu}$

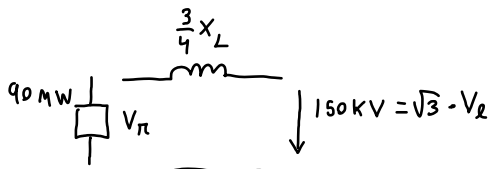
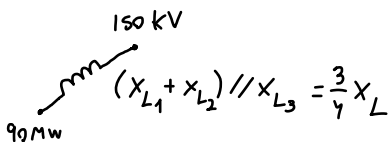
$$x_{th} = x_c + x_b + 0,2 = \frac{1}{2} x_L + \frac{1}{4} x_L + 0,2 = 0,325625$$

$$x_c = \frac{x_{L2} \cdot x_{L3}}{x_{L1} + x_{L2} + x_{L3}} = \frac{2 x_L^2}{4 x_L} = \frac{1}{2} x_L$$

$$x_b = \frac{x_{L1} \cdot x_{L3}}{x_{L1} + x_{L2} + x_{L3}} = \frac{x_L^2}{4 x_L} = \frac{1}{4} x_L$$



c)



$$\begin{cases} V_L = V_n + \frac{3}{4} X_L j \cdot I \\ 90 \text{ MW} = 3 \cdot V_n \cdot I^* \end{cases} \Leftrightarrow \begin{cases} \frac{150 \text{ kV}}{\sqrt{3}} = V_n + \frac{3}{4} \cdot 37,699 \cdot j \cdot I \\ 30 \text{ MW} = V_n \cdot I^* \end{cases}$$

a)

$$Z_L = j \cdot \omega \cdot L = j 6e.9964$$

$$Y_T = j \cdot \omega \cdot C = j 75.4 \times 10^{-3}$$

$$P_m = \frac{V_m^2}{Z_0} = \frac{V_m^2}{\sqrt{\frac{L}{C}}} = 170 \text{ MW}$$

b)

$$A = \cos(\beta d)$$

$$B = j Z_0 \sin(\beta d)$$

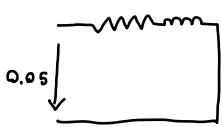
$$C = j \frac{1}{Z_0} \sin(\beta d)$$

$$\begin{bmatrix} A & B \\ C & A \end{bmatrix} \cdot \begin{bmatrix} 220 \text{ kV} \\ \frac{300 \text{ M}}{3 \cdot 220 \text{ K}} \end{bmatrix} = 7 V_L = 230.24 \text{ kV}$$

c) $V_L = 230.243 \text{ kV}$

$$I_L = 775.124 \text{ A}$$

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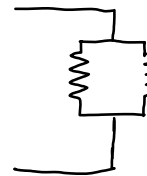


$$P_{cc} = R_t \cdot I_m^2 \Leftrightarrow R_t = 0.005 \mu$$

$$Z_t = \frac{V_{cc}}{I_m} = 0.05$$

$$X_t = \sqrt{0.05^2 - 0.005^2} = 0.0497 \mu$$

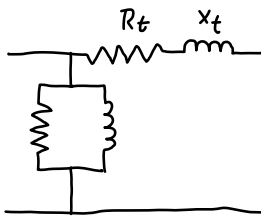
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$$P_o = G_m V_o^2 \Leftrightarrow G_m = 0.0025 \mu$$

$$Y_m = \frac{I_o}{V_m} = \frac{100}{\frac{200 \text{ M}}{\sqrt{3} \cdot 10 \text{ K}}} = 0.00866 \mu$$

$$B_m = -\sqrt{Y_m^2 - G_m^2} = -0.00829 \mu$$



$$P_{Cu} = R_t \cdot I^2 = 0.005 \cdot \left(\frac{775.124}{\frac{200 \text{ M}}{\sqrt{3} \cdot 220 \text{ K}}} \right)^2 = 0.002726 \mu \rightarrow 0.545 \text{ MW}$$

$$P_{Fe} = G_m \cdot V^2 = 0.0025 \cdot \left(\frac{230.243 \text{ kV}}{220 \text{ kV}} \right)^2 = 0.002738 \mu \rightarrow 0.548 \text{ MW}$$