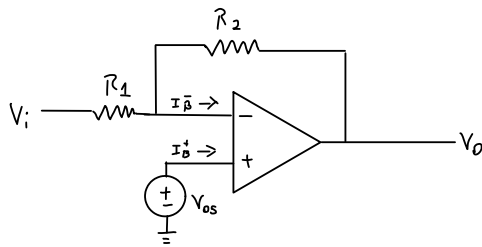


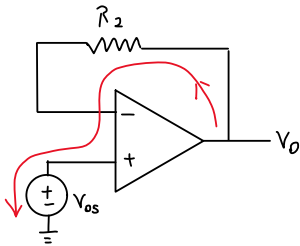
1. $G = -100$

a) $R_1 = 100 \text{ k}\Omega$

b) $R_2 = 10 \text{ M}\Omega$



$V_i \Rightarrow C.A.$



$V_o = 5.3 \text{ V}$

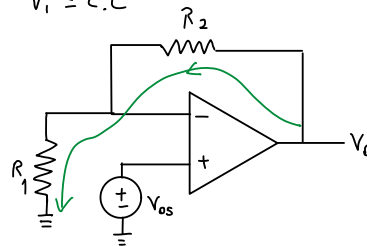
$* V_o - R_2 I_2 - V_{os} = 0$

$\text{Mas } I_2 = I_B^-!$

Logo

$V_o = R_2 I_B^- + V_{os}$

$V_i = C.C$



$V_o = 5 \text{ V}$

$* V_o - V^- = R_2 I_2 \Leftrightarrow$

$\Leftrightarrow V_o - V^+ = R_2 (I_B^- + I_1) \Leftrightarrow$

$\Leftrightarrow V_o - V_{os} = R_2 (I_B^- + \frac{V_{os}}{R_1}) \Leftrightarrow$

$\Leftrightarrow V_o = V_{os} (1 + \frac{R_2}{R_1}) + R_2 I_B^-$

$I_2 = I_B^- + I_1$

$V^+ = V^- = V_{os}$

$I_1 = \frac{V_{os}}{R_1}$

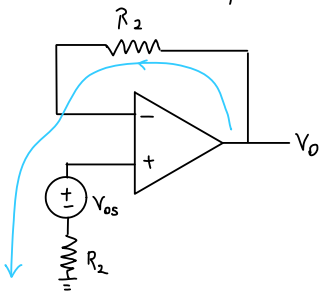
$I_B = \frac{I_B^- + I_B^+}{2} \approx 530 \text{ nA} //$

$V_o = R_2 I_B^- + V_{os}$

$V_o = V_{os} (1 + \frac{R_2}{R_1}) + R_2 I_B^-$

$\Leftrightarrow \begin{cases} V_{os} = -3 \text{ mV} // \\ I_B^- = 530 \text{ nA} \end{cases}$

c)

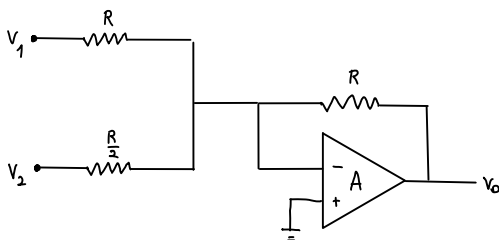


$* V_o = R_2 I_B^- + V_{os} - R_2 I_B^+ \Leftrightarrow$

$\Leftrightarrow \frac{V_o - R_2 I_B^- - V_{os}}{R_2} = I_B^+ = 589.7 \text{ nA} \approx 590 \text{ nA}$

$I_{os} = |I_B^+ - I_B^-| = 60 \text{ nA}$

2

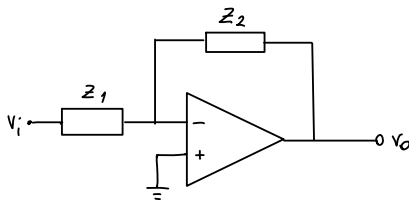


$\begin{cases} \frac{V_1 - V^-}{R} + \frac{V_2 - V^-}{R_2} + \frac{V_o - V^-}{R} = 0 \\ A(V^+ - V^-) = V_o \end{cases}$

$\Leftrightarrow \begin{cases} V_1 + 2V_2 + V_o = 4V^- \\ V_o = -AV^- \end{cases}$

$\Rightarrow V_o = -A \frac{V_1 + 2V_2 + V_o}{4} \Leftrightarrow V_o = -(V_1 + 2V_2) \frac{A}{4 + A} //$

3. a)



$$\begin{cases} \frac{V_o}{V_i} = -\frac{Z_2}{Z_1} \\ Z_2 = R_2 \parallel \frac{1}{j\omega C_2} = \frac{1}{\frac{1}{R_2} + j\omega C_2} = \frac{R_2}{1 + j\omega C_2 R_2} \\ Z_1 = R_1 \parallel \frac{1}{j\omega C_1} = \frac{R_1}{1 + j\omega C_1 R_1} \end{cases} \Rightarrow \frac{V_o}{V_i} = -\frac{R_2}{R_1} \cdot \frac{1 + j\omega C_1 R_1}{1 + j\omega C_2 R_2} = -\frac{C_1}{C_2} \cdot \frac{\frac{1}{C_1 R_1} + j\omega}{\frac{1}{C_2 R_2} + j\omega} \Rightarrow \begin{cases} \omega_z = \frac{1}{C_1 R_1} \\ \omega_p = \frac{1}{C_2 R_2} \\ DC = -\frac{R_2}{R_1} \quad \omega \rightarrow 0 \\ HF = -\frac{C_1}{C_2} \quad \omega \rightarrow \infty \end{cases}$$

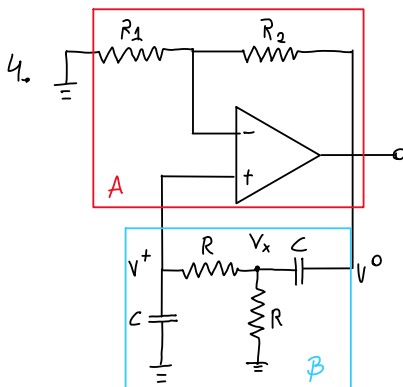
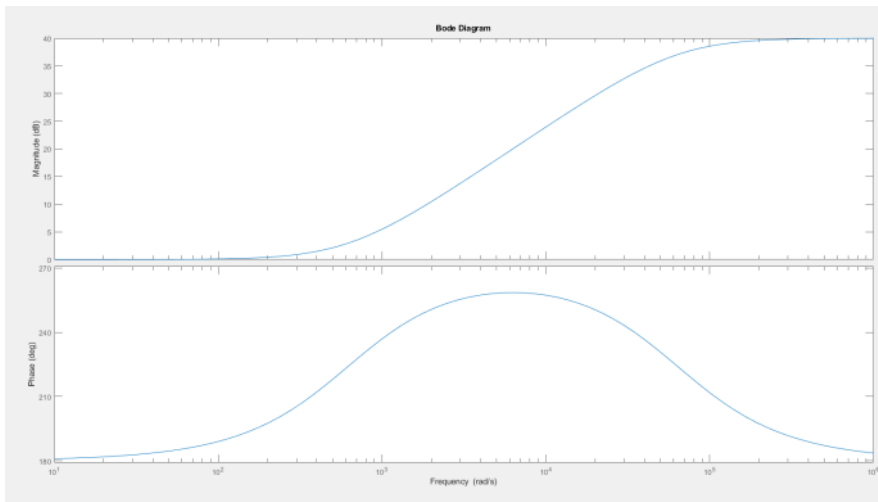
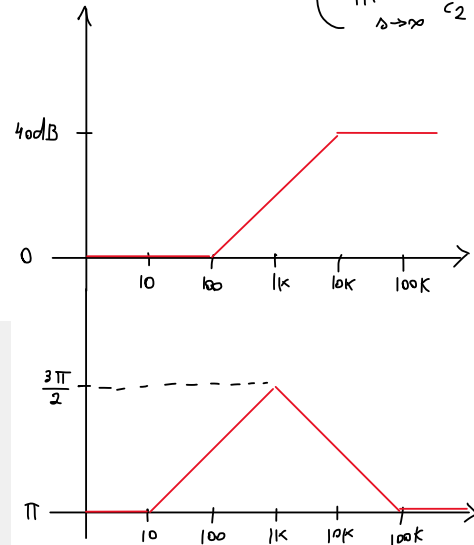
b) $\omega_z = 2\pi \cdot 100 \Rightarrow C_1 = \frac{1}{R_1 \omega_z} = 160 \text{ nF}$

$\omega_p = 2\pi \cdot 10 \cdot 10^3 \Rightarrow C_2 = \frac{1}{R_2 \omega_p} = 1.60 \text{ nF}$

$|DC| = 1 \Rightarrow R_2 = 10 \text{ k}\Omega$

$R_{in} = 10 \text{ k}\Omega \Rightarrow R_1 = 10 \text{ k}\Omega$

$\Rightarrow |HF| = 100$



A: Montagem não inversora

$$A = 1 + \frac{R_2}{R_1}$$

B: $\beta = \frac{V^+}{V_o} = \frac{\Delta CR}{\Delta^2 C^2 R^2 + 3\Delta CR + 1}$

$$V^+ = \frac{\frac{1}{\Delta C}}{\frac{1}{\Delta C} + R} \cdot V_x = \frac{1}{1 + \Delta CR} V_x$$

$$V_x = \frac{(R+C) \parallel R}{(R+C) \parallel R + C} V_o = \frac{\frac{\Delta CR^2 + R}{2\Delta CR + 1}}{\frac{\Delta CR^2 + R}{2\Delta CR + 1} + \frac{1}{\Delta C}} V_o = \frac{\Delta^2 C^2 R^2 + \Delta CR}{\Delta^2 C^2 R^2 + 3\Delta CR + 1} V_o$$

$$\begin{aligned} (R+C) \parallel R &= \left[\left(R + \frac{1}{\Delta C} \right)^{-1} + R^{-1} \right]^{-1} = \left[\frac{\Delta C}{\Delta CR + 1} + \frac{1}{R} \right]^{-1} = \\ &= \frac{1}{\frac{\Delta C}{\Delta CR + 1} + \frac{1}{R}} = \frac{R(\Delta CR + 1)}{\Delta CR + \Delta CR + 1} = \\ &= \frac{\Delta CR^2 + R}{2\Delta CR + 1} \end{aligned}$$

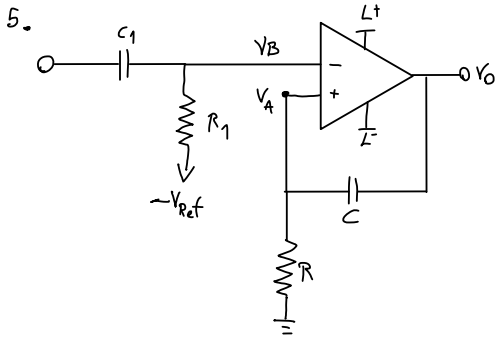
$$L(\Delta) = A\beta = \left(1 + \frac{R_2}{R_1} \right) \cdot \frac{\Delta CR}{\Delta^2 C^2 R^2 + 3\Delta CR + 1}$$

$$V^+ = \frac{1}{1 + \Delta CR} \cdot \frac{\Delta CR(1 + \Delta CR)}{\Delta^2 C^2 R^2 + 3\Delta CR + 1} V_o = \frac{\Delta CR}{\Delta^2 C^2 R^2 + 3\Delta CR + 1} V_o$$

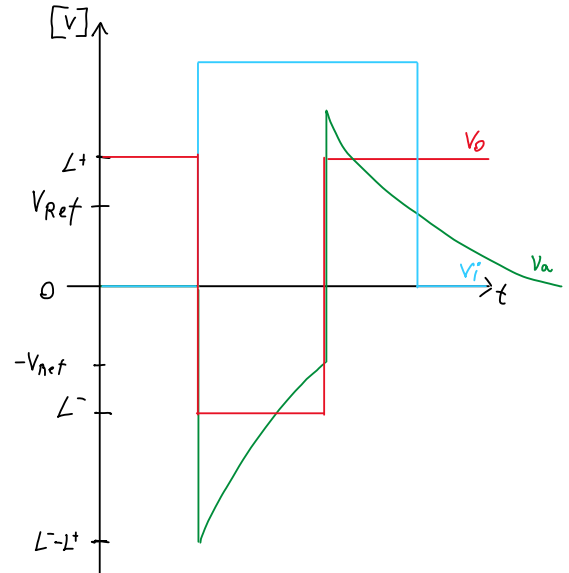
$$L(b) = A\beta = \left(1 + \frac{R_2}{R_1}\right) \cdot \frac{\omega CR}{\omega^2 C^2 R^2 + 3\omega CR + 1} = 1$$

$$\left(1 + \frac{R_2}{R_1}\right) \cdot \frac{j\omega CR}{-\omega^2 C^2 R^2 + 3j\omega CR + 1} = 1$$

$$\left(1 + \frac{R_2}{R_1}\right) \cdot \frac{\omega CR}{-\frac{1}{j}\omega^2 C^2 R^2 + 3\omega CR + \frac{1}{j}} = 1 \Rightarrow \begin{cases} -\frac{1}{j}\omega^2 C^2 R^2 + \frac{1}{j} = 0 \Leftrightarrow \omega^2 C^2 R^2 = 1 \Rightarrow \omega = \frac{1}{CR} \\ \frac{(1 + \frac{R_2}{R_1})\omega CR}{3\omega CR} = 1 \Rightarrow \frac{R_2}{R_1} = 2 \end{cases}$$



$$\begin{aligned} V_O &= L^+ \\ V_A &= 0 \\ V_B &= -V_{ref} \end{aligned}$$



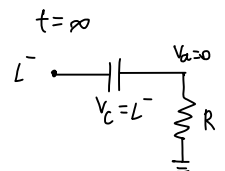
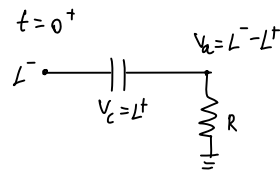
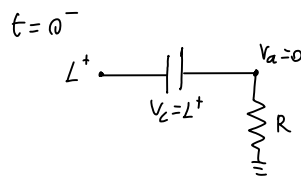
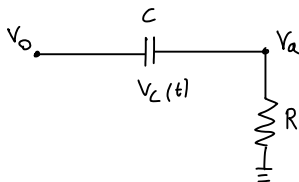
$$V_i > V_{ref} \Rightarrow V_B > 0 \Rightarrow V_O \rightarrow L^-$$

$$V_C = L^+ \text{ (Não muda instantaneamente!)}$$

$$V_A = V_O - V_C = L^- - L^+ \Rightarrow \text{C vai descarregar até atingir } V_A = -V_{ref}$$

$$\text{Como } V_B \text{ é momentânea } V_B = V_{ref}, V_O \text{ passa de } L^- \text{ para } L^+$$

$$V_A = V_O - V_C = L^+ - (L^- - V_{ref}) = L^+ - L^- - V_{ref}$$



$$V_A = RC \frac{dV_C}{dt} \quad \begin{aligned} V_A(0^+) &= L^- - L^+ & K_2 &= L^- - L^+ \\ V_A(\infty) &= 0 & K_1 &= 0 \end{aligned}$$

$$V_A(t) = K_1 + K_2 e^{-\frac{t}{RC}} \Rightarrow V_A(t) = (L^- - L^+) e^{-\frac{t}{RC}} \Rightarrow -V_{ref} = (L^- - L^+) e^{-\frac{t}{RC}} \\ \hookrightarrow t = RC \ln\left(\frac{L^+ - L^-}{V_{ref}}\right)$$