



$$\begin{cases} \frac{\partial \bar{V}}{\partial z} = -R \bar{I} - L \frac{\partial \bar{I}}{\partial t} \\ \frac{\partial \bar{I}}{\partial z} = -G \bar{V} - C \frac{\partial \bar{V}}{\partial t} \end{cases}$$

$$\begin{cases} \frac{\partial^2 \bar{V}}{\partial z^2} = (R + j\omega L)(G + j\omega C) \bar{V} \\ \frac{\partial^2 \bar{I}}{\partial z^2} = (R + j\omega L)(G + j\omega C) \bar{I} \end{cases}$$

$$\bar{V}(d) = \bar{V}_i + \bar{V}_r = \bar{V}_{i0} e^{\gamma d} + \bar{V}_{r0} e^{-\gamma d}$$

$$\begin{aligned} \bar{I}(d) &= \bar{I}_i + \bar{I}_r = \bar{I}_{i0} e^{\gamma d} + \bar{I}_{r0} e^{-\gamma d} \\ &= \frac{\bar{V}_{i0}}{Z_0} e^{\gamma d} - \frac{\bar{V}_{r0}}{Z_0} e^{-\gamma d} \end{aligned}$$

$$\bar{V}_r = \bar{V}^- \quad \bar{V}_i = \bar{V}^+ \quad \bar{I}_r = \bar{I}^- \quad \bar{I}_i = \bar{I}^+$$

$$\begin{aligned} \bar{V}_{i0} &= \frac{1}{2} (V_L + I_L Z_0) \\ \bar{V}_{r0} &= \frac{1}{2} (V_L - I_L Z_0) \end{aligned}$$

$$\gamma = \alpha + j\beta = \sqrt{(R + j\omega L)(G + j\omega C)}$$

$$\frac{\bar{V}_i}{\bar{I}_i} = -\frac{\bar{V}_r}{\bar{I}_r} = Z_0 \quad Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$$

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$$\begin{cases} R=0 \\ G=0 \end{cases} \Rightarrow \begin{cases} \frac{\partial \bar{V}}{\partial z} = -L \frac{\partial \bar{I}}{\partial t} \\ \frac{\partial \bar{I}}{\partial z} = -C \frac{\partial \bar{V}}{\partial t} \end{cases} \Rightarrow \frac{\partial^2 \bar{V}}{\partial z^2} = LC \frac{\partial^2 \bar{V}}{\partial t^2}$$

$$V_p = \frac{1}{\sqrt{LC}}$$

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$$\begin{aligned} Z(d) &= \frac{\bar{V}(d)}{\bar{I}(d)} = Z_0 \frac{Z_L + Z_0 \tanh(\gamma d)}{Z_0 + Z_L \tanh(\gamma d)} \\ &= Z_0 \frac{1 + K_V(d)}{1 - K_V(d)} \end{aligned}$$

$$K_V(d) = \frac{\bar{V}_r(d)}{\bar{V}_i(d)} = K_V(0) e^{-2\gamma d}$$

$$K_V(d) = \frac{\bar{V}_r(d) - 1}{\bar{V}_i(d) + 1} = \frac{Z(d) - Z_0}{Z(d) + Z_0}$$

$$\bar{V}_i(d) = \frac{Z(d)}{Z_0} = \frac{1 + K_V(d)}{1 - K_V(d)}$$

$$K_V(0) = \frac{Z_L - Z_0}{Z_L + Z_0}$$

$$\alpha=0 \quad Z(d) = Z_0 \frac{Z_L + jZ_0 \tan(\beta d)}{Z_0 + jZ_L \tan(\beta d)}$$

$$Z(d) = Z(d + n\frac{\lambda}{2})$$

$$\beta d \ll \pi \rightarrow Z(d) = Z_L$$

$$l = \frac{\lambda}{4} \rightarrow Z(l) = \frac{Z_0^2}{Z_L}$$

$$\lambda = \frac{\lambda}{2} \rightarrow Z(\lambda) = Z_L$$

$$Z_L = Z_0 \rightarrow Z(d) = Z_0$$

$$Z_L = 0 \rightarrow Z(d) = jZ_0 \tan(\beta d) = jX$$

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$$P(d) = \frac{1}{2} \operatorname{Re} \{ \bar{V}(d) \cdot \bar{I}^*(d) \} = P^+ + P^-$$

$$P^+ = \frac{1}{2} \frac{|\bar{V}^+|^2}{Z_0} \quad P^- = -\frac{1}{2} \frac{|\bar{V}^-|^2}{Z_0}$$

$$P(d) = P^+ (1 - |K_V|^2) \quad |K_V|^2 = \left| \frac{\bar{V}^-}{\bar{V}^+} \right|^2$$

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$$SWR = \frac{V_{max}}{V_{min}} = \frac{1 + |K_V|}{1 - |K_V|} \quad |K_V| = \frac{SWR - 1}{SWR + 1}$$

$$V_{max} = |V^+| (1 + |K_V|) \quad V_{min} = |V^+| (1 - |K_V|)$$

$$I_{max} = \frac{|V^+|}{Z_0} (1 + |K_V|) \quad I_{min} = \frac{|V^+|}{Z_0} (1 - |K_V|)$$

$$Z_{max} = Z_0 \cdot SWR \quad Z_{min} = \frac{Z_0}{SWR}$$

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ZY

$$C.C. \quad K_V = -1 \quad SWR = \infty \quad \times \cdot \times$$

$$C.A. \quad K_V = 1 \quad SWR = \infty \quad \times \cdot \times$$

$$A \quad K_V = 0 \quad SWR = 1 \quad \cdot \times \cdot$$

$$\leftarrow \Rightarrow \begin{cases} V_{min} & I_{max} & Z_{min} & (Z) \\ V_{max} & I_{min} & Y_{min} & (Y) \end{cases}$$

$$\rightarrow \Rightarrow \begin{cases} V_{max} & I_{min} & Z_{max} & (Z) \\ V_{min} & I_{max} & Y_{max} & (Y) \end{cases}$$

$$y_{im} = 1 \Rightarrow y_{st} + y'_{im} = 1$$

$$y_{st} = -\frac{j}{\tan(\beta l)} = -j \cotan(\beta l)$$

$$y'_{im} = 1 - j \cotan(\beta l) \Rightarrow \operatorname{Re} \{ y'_{im} \} = 1$$

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$$C_0 = 3 \times 10^{-8} \quad \mu_0 = 4\pi \times 10^{-7} \quad \epsilon_0 = \frac{10^{-4}}{36\pi}$$

$m = 10^{-3}$	$K = 10^3$	$\beta = \frac{2\pi}{\lambda}$
$\mu = 10^{-6}$	$M = 10^6$	$v_f = \frac{\omega}{\beta}$
$m = 10^{-9}$	$G = 10^9$	$v_g = \frac{d\omega}{d\beta}$
$p = 10^{-12}$	$T = 10^{12}$	
$f = 10^{-15}$	$P = 10^{15}$	$c = \lambda f$